

## NAVIER-OVO RESENJE

$$w(x, y) = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} A_{mn} \cdot \sin\left(\frac{m\pi x}{a}\right) \sin\left(\frac{n\pi y}{b}\right)$$

$$A_{mn} = \frac{Z_{mn}}{K\pi^4 \left( \frac{n^2}{b^2} + \frac{m^2}{a^2} \right)^2}$$

$$Z_{mn} := \frac{4}{a \cdot b} \left( \int_0^a \int_0^b Z(x, y) \sin\left(\frac{m\pi x}{a}\right) \sin\left(\frac{n\pi y}{b}\right) dx dy \right)$$

## MORIS-LEVY

$$W = W_1 + W_0$$

$$Y_n(y) = \left( A_n + \frac{n\pi y}{a} B_n \right) \cosh \frac{n\pi y}{a} + \left( C_n + \frac{n\pi y}{a} D_n \right) \sinh \frac{n\pi y}{a}$$

$$W_1 = \sum_{n=1}^{\infty} Y_n(y) \cdot \sin \frac{n\pi x}{a}$$

$$W_0 = \sum_{n=1}^{\infty} W_{0n} \cdot \sin \frac{n\pi x}{a}$$

$$W_{0n} = \frac{Z_n \cdot a^4}{K n^4 \pi^4}$$

$$Z_n = \frac{2}{a} \cdot \int_0^a Z(x) \sin \frac{n\pi x}{a} dx$$

$$W(x, y) = W_0 + W_1 =$$

$$\sum_{n=1}^{\infty} \left( \frac{Z_n \cdot a^4}{K n^4 \pi^4} + \left( A_n + \frac{n\pi y}{a} B_n \right) \cosh \frac{n\pi y}{a} + \left( C_n + \frac{n\pi y}{a} D_n \right) \sinh \frac{n\pi y}{a} \right) \cdot \sin \frac{n\pi x}{a}$$

- simetrično opterećenje  $A_n$  i  $D_n$
- antisimetrično opterećenje  $B_n$  i  $C_n$  (g.u.  $Y = \pm b/2$ )

## PLOCA OSLONJENA NA GREДУ

$$Y = (1)w^p = w^g \Rightarrow \frac{dW_{pl}}{dx^4} = \frac{dW_{gr}}{dx^4} \quad (2) \frac{dW_{pl}}{dy} = j_g \Rightarrow \frac{d^2 W_{pl}}{dx dy} = \frac{dj_g}{dx} = q = \frac{Mt}{GIt}$$

$$(1) \Rightarrow \frac{d^4 W_{pl}}{dx^4} = \frac{\bar{T}_y}{EIg} = \frac{-K}{EIg} \left( \frac{d^3 W_{pl}}{dy^3} + (2-u) \cdot \frac{d^3 W_{pl}}{dx^2 dy} \right)$$

$$(2) \Rightarrow \frac{d}{dx} \left( GIt \cdot \frac{d^2 W_{pl}}{dx dy} \right) = \frac{dMt}{dx} = M_y = -K \left( \frac{d^2 W_{pl}}{dy^2} + u \frac{d^2 W_{pl}}{dx^2} \right)$$

## SILE U PRESEKU

$$M_x = -K \left( \frac{d^2 W}{dx^2} + u \frac{d^2 W}{dy^2} \right)$$

$$M_y = -K \left( \frac{d^2 W}{dy^2} + u \frac{d^2 W}{dx^2} \right)$$

$$M_{xy} = -K(1-u) \frac{d^2 W}{dx dy}$$

$$\bar{T}_x = -K \left[ \frac{d^3 W}{dx^3} + (2-u) \frac{d^3 W}{dx dy^2} \right]$$

$$\bar{T}_y = -K \left[ \frac{d^3 W}{dy^3} + (2-u) \frac{d^3 W}{dx^2 dy} \right]$$